

STABILIZATION OF THE EXTERNAL TANK FOR USE AS A LARGE SPACE PLATFORM

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Abstract

Use of magnetic passive dampers is recommended to stabilize the Space Shuttle External Tank in free flight for on-orbit applications. Longitudinal alignment along the radius vector allows for gravity gradient passive stabilization, but, without a damping mechanism, there is no inherent means of eliminating disturbance accelerations and buildup of pendular motions lead to spin or tumbling. Review of previous magnetic, passive dampers is provided drawing from the Long Duration Exposure Facility (LDEF) flight and Space Station program studies for early assembly flights. Basic physical models of the damper-spacecraft combination are discussed; damper capabilities and limitations. Preliminary damper design analysis is demonstrated.

Introduction

Medieval alchemists who sought transform of lead into gold would find accord with seekers of useful orbital payloads derived from expended rocket propellant tanks. For decades designers have considered spent rocket stages for space applications, thus combining launch and mission structural functions, the Skylab space station a notable example. Since Space Shuttle formulation as a space plane with an expendable External Tank (ET) jettisoned at suborbital velocity, it has attracted numerous proposals for delivering the ET (Fig.-1) into orbit as a space platform.

Advocates have proposed its large fuel and oxidizer tanks as pressurized laboratories^{1,2} or micro-g processing plants; they also note the dynamic stability of a symmetric cylindrical form (gravity gradient stabilization), the prospect of scavenging residual propellant, using intertank position mounts for external payloads and even exploiting the ET as an on-orbit scrap metal source. Studies have included a gamma ray observatory (ET-GRO), industrial processing facilities, an orbital fluid storage tank, a "strong back" for mounting other devices, a counter weight for tethered boost (and consequent ET de-orbit) of other payloads and even space station concepts. Plans have ranged from those requiring only one Shuttle flight and release before operations (e.g., ET-GRO) to those involving revisits or assembly mission sequences.

Whether ET applications involve single or multiple flights for setting up space platforms, proposals still encounter thorny problems. Functional simplicity of the ET prevents tapping into readily available utilities for propulsion, attitude control, communications and power generation; ET structures and materials were chosen to store propellant for a 10 minute ascent - and little else. To counter these issues, designers have proposed a number of fixes, but to our knowledge, none has suggested magnetic damper use for passive stabilization. Discussion of the capabilities, limitations and modeling of dampers for the ET follows.

Cylindrical or ellipsoidal satellites with corresponding mass properties can be stabilized with respect to the local vertical - local horizontal (LVLH) if their principal (inertia) axes are placed near stability points: the minimum inertia axis, along the radius vector \underline{R} ; the intermediate, along velocity vector \underline{V} ; and maximum with orbital plane normal \underline{N} ($I_{pitch} > I_{roll} > I_{yaw}$ or $I_N > I_T > I_R$). Gravity gradient (g.g.) forces tend to counter deflections in roll and pitch (rotations about the orbital tangential \underline{V} and \underline{N} , if the body coordinates deflections from local coordinates are small), but neither low earth orbit (LEO) aerodynamics or rigid body mechanics provide any inherent damping to perturbations induced. There can be a host of reasons for a spacecraft to begin oscillations: variations in the minuscule aerodynamic moments, departure from circular orbit due to Keplerian eccentricity or gravity field oblateness effects, thermal buckling with passage in and out of the Earth's shadow, fluid venting, initial spacecraft release conditions or subsequent mechanical history. Generally, to counter these effects, designers employ active means of control such as attitude thrusters, reaction wheels or control moment gyros (CMGs) which presuppose fuel systems or power supplies. Even magnetic torquer bars, used on the Hubble Space Telescope to desaturate the reaction wheel primary control system, require current from an external power source to regulate their response.

An early Space Shuttle payload employed a notable exception to these "active" control schemes. In April, 1984 the Long Duration Exposure Facility (LDEF, Fig.-2) was launched, a passively stabilized 11-ton cylindrical satellite with a 12-sided longitudinal cross-

section. This satellite orbited for several years in LEO without tumbling or accumulating large angular rates until January 1990 (STS-32) retrieval. The presence of large bar magnets embedded in one of two concentric spheres accounted for its stability; the cluster positioned itself in alignment, (described in ³⁻⁶) with the terrestrial magnetic field, impeded by a viscous fluid layer between the two spherical shells (Fig.-3). From the perspective of the spacecraft, if the magnetic damper is sized appropriately, perturbing accelerations and motions from the LVLH are damped and eventually decay. A terrestrial analog to a spacecraft with a passive magnetic damper would be a ship with an anchor that simply impedes its tendency to drift by dragging on a muddy sea bottom; the anchor does not really “anchor” the ship in this case, but slows it down.

Beside application to LDEF, this stabilization method was extensively studied for the first Space Station Freedom assembly flight; perhaps for several flights if power and control were unavailable and the application proved effective. During these studies, means were developed to determine the size of the magnetic dampers required and simulate their performance on orbit at various levels of fidelity. The author participated in the Space Station control studies as well as several earlier, unrelated ET applications studies⁷ in which dampers were not considered. He sees no reason that LDEF and Space Station experience can not be applied to the ET stabilization problem. For that matter, magnetic dampers would probably work as effectively on other spent upper stages (e.g., Titan, Ariane or Proton), if similar applications were proposed.

In the summer of 1986, this analyst and several colleagues⁸⁻¹⁰ examined tentative schemes for passive stabilization of early Space Station assembly flights, concluding that magnetic passive dampers were the best means available. Subsequent analyses drew on the earlier LDEF work of Old Dominion University researchers Heinbockel and Breedlove^{3,4} as well as Dr. Karen Castle's preceding LDEF contractor work at the Johnson Space Center. We first assessed damper gain requirements with root locus stability analyses, then developed 6-degree of freedom simulations of spacecraft damper control. Our initial simulations employed simple cylinder and plate aerodynamics and a dipole model of terrestrial magnetism without offset from the earth's center, but inclined to the axis of rotation¹¹. Later simulations included a detailed geophysical field model and aerodynamics closely based on CAD modeling¹². Pilot-in-the-loop flight simulator

runs modeled thruster plume impingement effects of the Orbiter separation maneuver as well as residual rates from separation with the Shuttle Remote Manipulator System (RMS)¹³. Finally, studies were undertaken to determine the effect of modeling both the spacecraft and the field tracking magnet. Once again, a root locus concept was developed as well as detailed dynamic simulations^{14,15}.

The dynamic simulations noted above involve various levels of fidelity, but analyses with preliminary design tools are just as important as detailed configuration examinations. There are hardware limitations in constructing stiff magnetic damper systems, but in theory a magnetic damper could become so tight that it would align the vehicle with the magnetic pole. At lower gains steady state errors could also be very high, precluding the use of mission-oriented instrumentation, or else the action of seeking magnetic alignment could induce resonant oscillations of exactly the sort which mission planners sought to avoid. Root locus plots, for example, identify suitable control gains, eliminating need for global search with 6-DOF simulation. Formulation of the linearized system in the Laplace domain gives an indication of time dependent behavior based on initial conditions. Lyapunov stability analysis, based on Lagrangian and Hamiltonian dynamics, determines initial deflection and rate bounds for tumbling or spinning about a point of stability. If rate and position stability limits can be determined from this analysis, deployment conditions for a passively stabilized spacecraft can be stipulated.

Early studies indicated that inclination effects tended to correspond to averaged *magnetic* latitude, since the the earth-fixed (but skewed) magnetic axis presented a varied incidence angle with respect to the satellite's plane over a day's rotation, disregarding nodal regression. With a nominal dipole 11.5° offset from the rotational axis, effective magnetic inclination varies above and below equatorial inclination by the same amount. Positions near the magnetic field equator reduce the damper's effectiveness.

It is possible to do only limited analysis of forcing functions without digital simulation. Atmospheric density variations in LEO can be attributed to latitude, altitude, solar extreme UV flux and geomagnetic variations in response to solar flares. If satellite cross sections change significantly with deflections, the effect of density variations can have differing effects on drag. Initially, for Space Station, we simulated spacecraft

with symmetric and simple geometric forms; we later discovered protuberances such as radiators broke the symmetry about the yaw axis, resulting in significant yaw-roll coupling motions generated by aerodynamic torque variations. Significant offsets of inertia axes from external geometries due to internal mass distributions introduced moment arms about the center of mass and asymmetric centers of pressure for port and starboard, zenith and nadir cross-sections of the vehicle. If there are significant discrepancies between the location and shape of the inertial ellipsoid (gravity gradient torques) and the surface contours (aerodynamic torques), a new balance of forces must be struck (e.g., Torque Equilibrium Attitude -TEA) or disturbance torques will continually toss the vehicle about.

Hardware Descriptions

Application of magnetic dampers to spacecraft depends on hardware issues: the technology for manufacturing the appropriate dampers, and the mass properties of the overall spacecraft to be stabilized. The nature of an ET application is largely conjecture, but initially the mass properties of an empty ET separated from the Orbiter will dominate dynamical considerations.

The *External Tank* is 154.2 ft tall and 27.5 ft in diameter and contains propellant for the Shuttle engines (SSMEs). The main components of the ET are a liquid O₂ tank, located in the forward position, an aft liquid H₂ tank and the intertank connecting the two. The intertank provides space for instrumentation plus attachment structures for the forward ends of the solid rocket boosters (SRBs). The ET carries 1,589,000-lbs of propellant. The H₂ tank is 2.5 times larger than the O₂ tank, but the O₂/H₂ load is 6:1 by weight. Tank structure is skin-stringer; thermal protection covering the tank exterior maintains propellant at cryogenic temperatures during the launch sequence and the 8.5 minute powered ascent. Feed lines to the SSMEs trail down the ET's side from the O₂ tank and protude from the base of the H₂ tank. Attach structures connect the Orbiter to the ET near the base feed lines and at the intertank. Active control mechanisms are located on the Orbiter.

Table-1 includes mass properties from¹⁶ for STS-44, a flight that used the nominal light weight tank design rather than the initial test flight version or the anticipated aluminum-lithium design (several tons heavier or lighter respectively). Note that Shuttle weight on this mission is 334,376.2-lbs prior to separation and 255,811 just after. This indicates an

expected 12,037 lbs of fluid to remain in the propellant tanks and lines, based on physical pumping constraints and margins to assure nominal targets. Note also, that the I_{xz} product of inertia for the ET is high relative to the longitudinal I_{xx} moment of inertia value.

LDEF was a 12-sided cylindrical, gravity-stabilized spacecraft host to 57 experiments, several characterizing the meteoroid and orbital-debris environment for the nominal 9-month mission (see Table-2). As a result of *LDEF*'s 5.7 year exposure time and heightened interest in the debris collisional threat, the entire spacecraft on retrieval was studied as a meteoroid and orbital-debris detector. Due to gravity-gradient orbital stabilization, the same general surfaces pointed into the velocity vector during the entire mission; its large exposed surface area (~130 m²) provided LEO particulate environment data, including directionality effects for both natural and man-made particles.

LDEF's viscous *magnetic damper* was contained in a spherical dome, fabricated from 1/32 inch thick 6061-T6 aluminum alloy sheet attached to a cylindrical base with aluminum screws. The cylindrical housing is a fiberglass structure, covered with aluminum tape, inside and outside, to meet thermal control requirements. The mounting plate material is 6061-T6 aluminum alloy, with the top and bottom surfaces also covered by aluminum tape. A thermistor mounted in the top center of the dome provided house keeping data. The assembled damper housing, with the damper inside, was mounted to a space end frame with stainless steel fasteners.

The aluminum-nickel-cobalt *LDEF* magnets exhibited a 2.2×10^5 pole-cm magnetic dipole moment (presumed strength coefficient of Alnico is 8; new materials¹⁷ such as NdFeB reach 30-45). Mechanical characteristics are approximate, but correspond to 1 ft-lb-sec damping capability in English units, if entered into a 2nd order mass-spring-damper system (one source: 5 Newton-m-sec or .37631 slug-ft²-sec). This coefficient is dimensionally similar to angular momentum, but corresponds to torque divided by angular rate in radians/sec. Damper gain in a deployed system can be controlled by the number and quality of dampers. For an individual damper

$$K_d = (8\pi/3)\mu r_o^4/\epsilon_o \quad (1.)$$

where μ is the fluid viscosity between spheres, r_o is the radius of the outer damper sphere, and ϵ_o is the

difference in radii between outer and inner spheres. To first order, increases of μ , outer sphere radius and proximity to inner sphere all tend to increase the damper gain, yet the strength of the magnet would be obliged to increase accordingly to maintain its orientation against the increasingly dissipative medium surrounding it. The manufacturer investigated a "super LDEF" damper with a factor of ten increase in performance. Ten-fold increase in K_d came with ten-fold increase in volume and dipole strength (2.2×10^6 pole-cm), but mass increased from 15 to 300-lbs. Extreme temperature variations could either alter the viscosity or freeze the working fluid and magnet. As a result, unless further testbed information is provided, some uncertainty remains in proportionalities between K_d , mechanical and magnetic properties.

For the baseline LDEF configuration and the two candidate spacecraft shown in Table-1 (the ET and Resource Node attached to the Russian FGB vehicle), damping time constants (t_d) can be compared as a function of damper gain (K_d) in ft-lb-secs. The ratios of the time constants are proportional to the principal inertias on the pitch axis, but higher orbital inclination for the International Space Station applications (51.6° vs. 28.5°) reduces the time constants to 63%. To obtain the same response from the ET as obtained by LDEF, the gain should be proportionately higher, depending on orbital inclination and principal inertias. It is suspected that an intermediate (e.g., 10 or 20x) gain would be adequate to prevent tumbling or excessive rate buildup. The natural frequency of any pendular motions are hardly affected by damping. The principal moments of inertia ratios dominate these oscillations vs. the influence of any attainable damping mechanism.

Dynamics and Coordinate Systems

Inclusion of a relatively simple device on board a spacecraft somehow elicits extensive discussion of space mechanics and environmental forces, but unlike some systems (e.g., tethers) the mechanics are not intractable. It is well worth questioning whether the mechanics of flight can be linearized in meaningful fashion, especially in stability studies. In the case of an attitude stabilized spacecraft, the pendular motions in the LVLH can be linearized much like a pendulum in terrestrial conditions. We noted already that averaged magnetic latitude describes the effectiveness of the magnetic damper since the likely dynamic time constant will be much longer than the period of LEO revolution, and the variations of magnetic inclination are $\pm 11.5^\circ$ of the nominal. Other approximations follow.

Coordinate systems for US manned spacecraft frequently borrow from aircraft conventions with the x along the longitudinal axis, the z toward the nadir in level flight and the y axis extended out the starboard wing to the pilot's right. The XYZ LVLH system in circular orbit coincides with this system, but these definitions are opposite in sign with the orbital normal \underline{N} and the radius vector \underline{R} . Stability orientation definitions depend more on the size of the principal axis inertia rather than its nomenclature, and in the ET case, g.g. stability is achieved by aligning the X axis along \underline{R} . Unless significant additional hardware is deployed to distinguish the I_z from I_y principal inertia, aligning the larger of the two with \underline{N} will provide only marginal inherent stability. Nonetheless, the body axes are now skewed with respect to LVLH, but we will refer for convenience to roll motion about the vector \underline{V} , pitch about the \underline{N} , and yaw about the \underline{R} vector, renaming the principal axes I_T , I_N and I_R accordingly. Additionally, re-defining the roll, pitch and yaw deflections for the minimum axis alignment along the radial, roll and pitch deflections exceeding 90° will signify uncontrolled tumbling; yaw deflections, spinning.

For a rigid body in circular orbit, the gravity gradient torque is in terms of principal inertia axes' deflections.

$$\underline{T}_{gg} = 3 \omega_o^2 \underline{R}_b \times \{I\} \underline{R}_b \quad (2a)$$

$$= 3 \omega_o^2 \begin{Bmatrix} (I_z - I_y) a_{23} & a_{33} \\ (I_x - I_z) a_{13} & a_{33} \\ (I_y - I_x) a_{13} & a_{23} \end{Bmatrix} = 3 \omega_o^2 \begin{Bmatrix} (I_R - I_N) s2\phi c^2\theta \\ (I_T - I_R) c\phi s2\theta \\ (I_N - I_T) s\phi s2\theta \end{Bmatrix} \quad (2b)$$

where ω_o is the orbital angular rate, $\{I\}$ the inertia tensor, \underline{R}_b the unit vector based on the rotation

$$\underline{R}_b = \{A\}_{ijk} \underline{R}_{LVLH} \quad (3)$$

The matrix $\{A\}_{ijk}$ is a rotational transformation sequence i-j-k from the LVLH unit vector frame. Resulting unit vector expressions depend on the rotational sequence selection; this is demonstrated by various deflection angle formulations in space mechanics literature for g.g. torques (discussed elsewhere¹⁸). Here we introduce the 1-2-3 yaw, pitch, roll sequence. Note that ψ is not explicit in eq. 2b, but ϕ and θ deflections induce yaw moments.

To determine the magnetic forces acting on a spacecraft, it is necessary to establish the position of the spacecraft \underline{R} and that of the Earth's magnetic polar axis

$\underline{N}_m(t)$ in inertial space. In the celestial sphere, angles analogous to terrestrial latitude and longitude define both vectors: declination δ and right ascension α , with subscripts M and R denoting magnetic pole and radius vectors respectively. Below, c and s denote cosine and sine.

$$\underline{R}(t) = (c\delta_R c\alpha_R, c\delta_R s\alpha_R, s\delta_R)^T, \quad (4.)$$

$$\underline{N}_M(t) = (c\delta_M c\alpha_M, c\delta_M s\alpha_M, s\delta_M)^T \quad (5.)$$

The damper motions are affected by the size of the magnetic torque term ΔT_d . This term originates in the interaction of the local terrestrial magnetic field strength with the intrinsic magnetic dipole of the bar magnet.

$$\underline{T}_d = \underline{\mu} \times \underline{B} = \begin{matrix} e_R & e_T & e_N \\ \mu_R & \mu_T & \mu_N; \\ B_R & B_T & B_N \end{matrix} \quad (6a.)$$

$$T_d = \text{abs}(\mu B) \sin \theta_M \quad (6b.)$$

where θ_M is due to the displaced orientation of the bar magnet from the terrestrial field lines.

The transformation from an LVLH orbital position frame to the inertial Cartesian coordinate frame with which eq. 3 corresponds (a 3-rotation matrix based on ascending node Ω , orbit inclination i , and circular arc along the orbital path from the ascending θ^*) is shown ineq. 7. Thus, unit vectors of the radius, horizontal or tranverse velocity and normal to the orbital plane (e_R , e_T , e_N) can be defined in terms of the transformation matrix of eq. 7 with the orbital angular parameters defining the difference between $\underline{R}(t)$ and $\underline{N}_M(t)$ in eq. 8.

$$\begin{matrix} I \\ [J \\ K \end{matrix} = \begin{matrix} (c\Omega c\theta^* - s\Omega c i s\theta^*) \\ \{ (s\Omega c\theta^* + c\Omega c i s\theta^*) \\ (s i s\theta^*) \end{matrix} \quad \begin{matrix} (-c\Omega s q^* - s\Omega c i c\theta^*) \\ (-s\Omega s\theta^* + c\Omega c i c\theta^*) \\ (s i c\theta^*) \end{matrix} \quad \begin{matrix} (s\Omega s i) \\ (-c\Omega s i) \\ (c i) \end{matrix} \} \quad \begin{matrix} e_R \\ [e_T] \\ e_N \end{matrix} \quad (7.)$$

$$\sin\phi_M(t) = \underline{R}(t) \bullet \underline{N}_M(t) =$$

$$c(\Omega - \alpha_M) c\delta_M c\theta^* - c(\Omega + \alpha_M) c i c\delta_M s\theta^* + s i s\delta_M s\theta^* \quad (8.)$$

Transformation of inertia matrix {I} to principal body axes and inertias with deflections involves solution of the inertial tensor eigenvalue problem. Stability alignment at I_R , I_T , I_N with initial coordinate axis deflections from LVLH to ψ_o , ϕ_o and θ_o depends on the selection of matrix $\{A\}_{ijk}$ as will the nature of the linearized equations of motion.

In the homogeneous linearized angular motion equations, we note the (possible) uncoupling of roll-yaw motions (9b&c) from the pitch plane (9a).

$$[I_N s^2 + \sin \phi_m K_d s + 3 \omega_b^2 (I_T - I_R)] \theta(t) = 0 \quad (9a.)$$

$$[I_T s^2 + 4 \cos^2 \phi_m K_d s + 4 \omega_b^2 (I_N - I_R)] \phi(t) +$$

$$[(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] s \psi(t) = 0 \quad (9b.)$$

$$[(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] s \phi(t) + \dots$$

$$[I_R s^2 + 2/3 \sin^2 \phi_m K_d s + \omega_b^2 (I_N - I_T)] \psi(t) = 0 \quad (9c.)$$

Transformations between time dependent and Laplace s- domain functions give specific solutions to equations of motion in terms of initial angular position and rate.

$$[I_N s^2 + \sin \phi_m K_d s + 3 \omega_b^2 (I_T - I_R)] \Theta(s) =$$

$$I_N(s \theta_o - d\theta_o/dt) + \sin \phi_m K_d \theta_o \quad (10a)$$

$$[I_T s^2 + 4 \cos^2 \phi_m K_d s + 4 \omega_b^2 (I_N - I_R)] \Phi(s) + \dots$$

$$[(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] s \Psi(s) =$$

$$I_T(s\phi_o - d\phi_o/dt) + 4 \cos^2 \phi_m K_d \phi_o + 1/3 \sin^2 \phi_m K_d \psi_o + [(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] \psi_o \quad (10b.)$$

$$[(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] s \Phi(s) + \dots$$

$$[I_R s^2 + 2/3 \sin^2 \phi_m K_d s + \omega_b^2 (I_N - I_T)] \Psi(s) = \dots$$

$$I_R (s \psi_o + d\psi_o/dt) + 2/3 \sin^2 \phi_m K_d \psi_o +$$

$$[(I_T - I_N + I_R) \omega_b - 1/3 \sin^2 \phi_m K_d] \phi_o \quad (10c.)$$

Thus, linearized equations for a rigid body on-orbit uncouple a 2nd order pitch [$\Theta(s)$ or $\theta(t)$] equation from the 4th order roll-yaw equations. Solutions of 2nd and 4th order systems in the s -plane have roots of the form

$$(s + \sigma_i + j \omega_{Ni})(s + \sigma_i - j \omega_{Ni}) = s^2 + 2\zeta_i \omega_{Ni} s + \omega_{Ni}^2 \quad (11.)$$

where $j = \sqrt{-1}$; ω_{Ni} , the natural frequency mode i ; and ζ_i , the characteristic damping of the resulting system. For oscillatory systems with $0 < \zeta_i < 1$, the homogeneous roots take the form

$$s_{12} = -\zeta_i \omega_{Ni} \pm j \omega_{Ni} (1 - \zeta_i^2)^{0.5} \quad (12.)$$

Thus, the pitch plane roots for non-zero damping have a real part, and an imaginary part, if $I_T > I_R$.

$$s_{12} = -\sin \phi_m K_d / I_N \pm j [3(I_T - I_R) / I_N]^{0.5} \dots \\ \times \{ 1 - (\sin \phi_m K_d)^2 / [(I_T - I_R) I_N] \}^{0.5} \quad (13.)$$

The pitch angle function dependencies become

$$\theta(t) = f(t, \phi_m, K_d, \theta_o, d\theta_o/dt, (I_T - I_R) / I_N) \quad (14.)$$

Assuming that the principal inertia about the radius vector is the minimum and that the gain K_d is a quantity smaller than the inertias, the pitch motions are oscillatory, damped only by the magnetic gain K_d .

$$\Theta(s) = \{ I_N(s \theta_o - d\theta_o/dt) + \sin \phi_m K_d \theta_o \} \dots \\ / [I_N s^2 + \sin \phi_m K_d s + 3 \omega_o^2 (I_T - I_R)] \quad (15a.)$$

$$\Theta(s) / I_N = \theta_o s / \{ [s + \zeta \omega_h + j \omega_N (1 - \zeta^2)^{0.5}] \dots \\ [s + \zeta \omega_h - j \omega_N (1 - \zeta^2)^{0.5}] \} + \dots \\ [\sin \phi_m K_d \theta_o / I_N] / \{ [s + \zeta \omega_N + j \omega_N (1 - \zeta^2)^{0.5}] \dots \\ \dots [s + \zeta \omega_N - j \omega_N (1 - \zeta^2)^{0.5}] \} \quad (15b.)$$

With $\omega_h = \omega_N (1 - \zeta^2)^{0.5}$, converting back to the t -domain

$$\theta(t) = \theta_o [\omega_h] \exp(-\zeta \omega_h t) \{ \cos(\omega_h t) + \dots \\ [(d\theta_o/dt) - \sin \phi_m K_d \theta_o / I_N] \sin(\omega_h t) / \omega_h \} \quad (16.)$$

The roll-yaw axis formulation is more complex, but amenable to the same analytical techniques adapted to

simultaneous linear differential equations. Conversion from the time domain to the Laplace domain establishes the role of the initial positions and rates. The resulting transfer function determinant in combination with the substitutions employed with Cramer's Rule define Laplace s -domain functions for $\Phi(s)$ and $\Psi(s)$. Conversion of the two sets of expressions to the time domain from the series of terms with the common 4th order denominators results in expressions of the form

$$\begin{bmatrix} b_{11} & b_{12} \\ b_{21} & b_{22} \end{bmatrix} \begin{bmatrix} \Phi(s) \\ \Psi(s) \end{bmatrix} = \begin{bmatrix} c_1 (\phi_o, \psi_o, d\phi_o/dt, d\psi_o/dt) \\ c_2 (\phi_o, \psi_o, d\phi_o/dt, d\psi_o/dt) \end{bmatrix} \quad (17.)$$

$$\phi(t) = \mathcal{L}^{-1} [(c_1 b_{22} - c_2 b_{12}) / (b_{11} b_{22} - b_{21} b_{12})] =$$

$$f(t, \phi_m, K_d, \phi_o, \psi_o, d\phi_o/dt, d\psi_o/dt, I_T, I_N, I_R) \quad (18a.)$$

$$\psi(t) = \mathcal{L}^{-1} [(b_{11} c_2 - b_{21} c_1) / (b_{11} b_{22} - b_{21} b_{12})] =$$

$$f(t, \phi_m, K_d, \phi_o, \psi_o, d\phi_o/dt, d\psi_o/dt, I_T, I_N, I_R) \quad (18b.)$$

Forcing functions independent of attitude (e.g., a pounding device, thermal excitations, orbital eccentricity) can be represented more easily, simply as functions of time. Paradoxically, *the damping in the linearized equations exists only if there is a magnetic field forcing function with time dependence related to orbital revolution and nodal regression ($\Omega(t)$)*. We expect $\sqrt{[(I_N - I_R) / I_T]}$ and $\sqrt{[(I_N - I_T) / I_R]}$ related roll and yaw motions with respect to orbital rate ω_o .

It is difficult to include aerodynamics in this linearized equation, unless the geometry of the vehicle is extremely simple. Deflections of θ, ϕ and ψ from the LVLH result in changed projections of plates or cylinders in \underline{V} , even if panels do not articulate. For a cylinder resembling the ET near its vacuum stability point, aero-moments on the cylindrical cross sections above and below the c.g. are likely to be unequal. LEO aerodynamics generally are modeled without damping forces based on free molecular flow dynamics. If the aerodynamics are largely in the pitch plane, gravity gradient torques will counter deflections, and the aero-moments themselves will decrease with the cosine of θ - which is not satisfactory for linear analysis. The presence of solar panels or radiators on ET applications could complicate the aerodynamics depending on their arrangement. At this point 6-DOF simulation of on-orbit dynamics are in order for most spacecraft for significant aero moments.

Linear stability limits should be considered as well. For the expression $(b_{11} b_{22} - b_{21} b_{12})$ in eqs. 18a and 18b, in the absence of damping, roots are imaginary, if the inertia ratios satisfy certain conditions. The oscillatory, linear nature of this relation breaks down, however, if angular position or velocity bounds are exceeded. Methods of analytical dynamics can provide indicators of bounds for angular rates and attitudes at which tumbling (pendulum pitch/roll) or spinning (yaw) would commence. Combinations of body rates ω or deflections represented by the a_{ij} cannot exceed total energy v .

$$v = \frac{(I_T \omega_T^2 + I_N \omega_N^2 + I_R \omega_R^2) / 2 + \dots}{\omega_o^2 \{ 3 [(I_T - I_R) a_{13}^2 + (I_N - I_Z) a_{23}^2] + \dots [(I_N - I_T) a_{12}^2 + (I_N - I_R) a_{32}^2] \} / 2} \quad (19.)$$

Owing to space limitations, we can only mention that conservative systems in rotating frames can be mapped out in phase space and that the 2nd order partials of the characteristic Hessian matrix must provide a positive definite matrix (see ^{19,18}). For yaw axis stability, and zero deflections, for example,

$$(I_T \omega_T^2 + I_N \omega_N^2 + I_R \omega_R^2) < \omega_o^2 (I_N - I_T) \quad \text{or}$$

$$[I_T (d\phi/dt - s\theta d\psi/dt)^2 + I_N (c\phi d\theta/dt + s\phi c\theta d\psi/dt)^2 + I_R (-s\phi d\theta/dt + c\phi c\theta d\psi/dt)^2] < \omega_o^2 (I_N - I_T) \quad (20.)$$

The most straight-forward example of position and velocity offsets from a stability point is that of 90° rotation of the 1st and 2nd largest principal inertias about the radial axis. This tends to reverse the signs of real roots. Plausible release conditions suggest that there will be high pitch deflection due to Shuttle longitudinal alignment with the velocity vs. radius vector, and considerable yaw deflection of the principal axis. We discuss these in the next section.

Finally, transition to stable orientation may experience spinning or tumbling transients. Much of the stability analysis makes little distinction between up or down pointing ETs, but payload instrumentation will without doubt. Some release conditions may be so extreme as to result in stabilization “upside down”, as we can show in the next section. This issue was also a fidelity concern for modeling both the spacecraft and the damper as separate bodies vs. a spacecraft and a magnet always aligned with the magnetic field. Dynamic simulation of spacecraft *and magnet* requires a time step significantly shorter than that required for

oscillations occurring at roughly orbital rate vs. those characterizing a bar magnet’s lag. Alternatively, linear analysis including the bar magnet increases the pitch eq. to 4th order, coupling pitch position of the body and magnet respectively (neglecting magnetic angular accelerations due to inertia ratio of magnet to body). Roll-yaw equations also increase in complexity.

Simulation Model and Results

Our 6-DOF simulation includes rotational rate and position initial conditions, orbital elements, varied gravity models, varied atmospheric density models and a rudimentary aerodynamic model comprised of cylindrical and flat plate elements. The ET surface could contribute significantly to any application aeromoments. Consequently, we divide this surface into two cylindrical centers of pressure located “above” and “below” the c.g. along the longitudinal axis. The moment arms of these surfaces, plus the optional solar flat plate solar panel models generate the aerodynamic moments at the end of moment arms projected into \underline{V} . Provision for unsymmetric radiators is achieved with paneling that minimizes its solar projection 90° out of phase of solar array rotation on one axis.

Disregarding pitch orientation, in the nominal ET separation (i.c.s), the Y and Z body axes are transposed so far as stability positioning is concerned; plus there is an additional offset 35° about the longitudinal axis to align the principal axis. These i.c.s make a good test case for damper effectiveness against spinning.

For discussion here we provide several ET test cases, isolating particular disturbance inputs and illustrating the attitude history in the absence or presence of magnetic dampers. In essence, this is a preliminary damper design exercise. The simplest case is the radial orientation of the ET in the Keplerian gravity field with the vehicle coordinates X,Y and Z aligned with \underline{R} , \underline{N} and \underline{V} providing a 35° deflection about yaw for the inertia axis and 1-2° for pitch and roll. This results in yaw axis (Fig.-4) oscillations that couple with pitch and roll in Figs. 5 and 6. Introduction of significant damping (50 ft-lb-secs) results in yaw stabilization about 90° deflection (Fig.-y) and reduced pitch-roll deflections. The yaw time constant is on the order of 10⁴ secs, and about 10⁵ secs on the other axes.

Testing the damper gain performance in the most benign environment: principal axes aligned with LVLH, no initial rates and no series expansion (J_2 , J_4 , etc.) of the gravity field, we note that damper gains induce steady

state pitch and roll oscillations, although 10, 20 and 50 ft-lb-sec dampers tend to capture the drifting yaw axis and stabilize it at 90° rotation. The steady state oscillations could be confused with orbital perturbations, using expanded gravity models. To reduce steady state oscillation, hardware complexity and mass, $K_d=10$ or 20 appears preferable to $K_d=50$.

The large product of inertia I_{xz} relative to I_{xx} tends to couple rotation about all 3 axes, counter to the linear theory discussed. In application, this could be countered by attaching payloads opposite to the side cluttered with propellant feed lines. Without any payload solar arrays, radiators or antennas, ET aerodynamics do not pose significant problems at high altitude or unexcited atmosphere. Addition of tracking solar arrays would tend to be destabilizing due to changing cross sections and rotor moments, but then the electrical power supplied could power an active control system such as reaction wheels or magnetic torquers which would supercede magnetic dampers.

Damping effectiveness against tumbling can be tested with nominal (vs. preferred - e.g., previous) pitch deflection at ET separation with the Orbiter aligned "head-down" to \underline{V} . Roll and pitch capture of the ET with the 3 different gains occurred after tumbling motion with large librations continuing on roll and pitch axes after 4×10^5 secs simulation time (Fig-7)). The crucial point here is that up or down capture cannot be assured unless initial pitch deflections are brought to lower levels (Figs.-8, -9). Fig. 8 also illustrates eq. 19. This is possible since the ET must be delivered into orbit first, before separation from the Orbiter can commence; this would allow maneuver to a more suitable pitch orientation (e.g., 45°).

Summary

We reviewed LEO delivery of the Space Shuttle External Tank and how its attitude can be stabilized using a previously applied technique, dissipation of disturbance torques with passive magnetic dampers. We have enumerated expected disturbances that could be encountered in deployment and during orbital motions, providing equations of motion and analytical tools for their description. Finally, based on hardware characteristics, we provided a preliminary damper design, attempting to minimize mass and magnet field strength by evaluating damping time constants and steady state errors.

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Table- 1 Mass Properties for Candidate Magnetic Damper Spacecraft

	ET empty, STS-44	LDEF	SSF MB-1	CETF (ca. 1987)	FGB/Node-1 (1996)
wgt -lbs	66,528	21,393	33,518		68,243
c.g. (inches - Shuttle System)		(Orbiter System)	(ft - SSF)	(ft-SSF)	(ft ISS)
x	1354.8	897	0.19		-40.71
y	2.7	0	117.45		.02
z	424.3	400	0.31		14.26

	Moments of Inertia (slug-ft**2)				(principal)
I _{xx}	354,005	24,090	215,000	4,707,760	66,269
I _{yy}	3,931,111	71,220	59,500	4,890,066	940,049
I _{zz}	3,929,108	73,270	227,000	339,673	951,860

	Products of Inertia (slug-ft**2)				
P _{xy}	3,692	3	26,800	-50,062	
P _{xz}	157,498	-4	-4,060	-293,556	(42,537)
P _{yz}	7,002	-6	-269	292,036	

	Deflection Angles from LVLH (assumes longitudinal coordinate axis aligned with radius vector, etc.)				
φ _o	-1.5	-	-	-	.13
θ _o	2.02	-	-	-	2.76
ψ _o	-35.12	.16	-	-	.01

NOTE: FGB/Node-1 combination characterizes the International Space Station at assembly stage 2 and illustrates an interesting magnetic damper candidate. This configuration is expected to be oriented in a spin stabilized mode supplemented by attitude control thrusters correcting precession. Studies of an 8-month delay in arrival of subsequent components indicated an 800-kg increase in the propellant budget for this operation, perhaps requiring an additional re-supply flight. Assuming thermal or other operational constraints could be overcome, magnetic dampers could save weight, propellant expenditures and mission costs.

Table-2 LDEF Specifications

Length:	30 feet (9.14 m)
Width:	14 feet (4.27 m)
Empty weight:	~9,000 pounds (3,629 kilograms)
Launch weight:	21,393 pounds (9,724 kilograms)
Experiment bays:	86 (72 peripheral & 14 end)
Number of experiments:	57
Deployment:	April, 1984; Challenger (STS-41C)
Retrieval:	January, 1990; Columbia (STS-32)
Orbital altitude:	216 - 154 nautical miles (400 - 286 kilometers); at deployment and retrieval, respectively
Exposed surface area:	~130 square meters

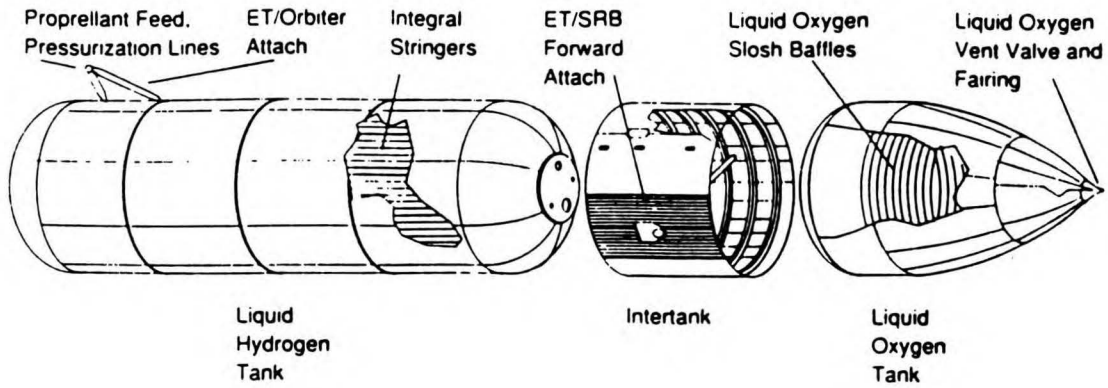


Fig-1 Space Shuttle External Tank (ET)

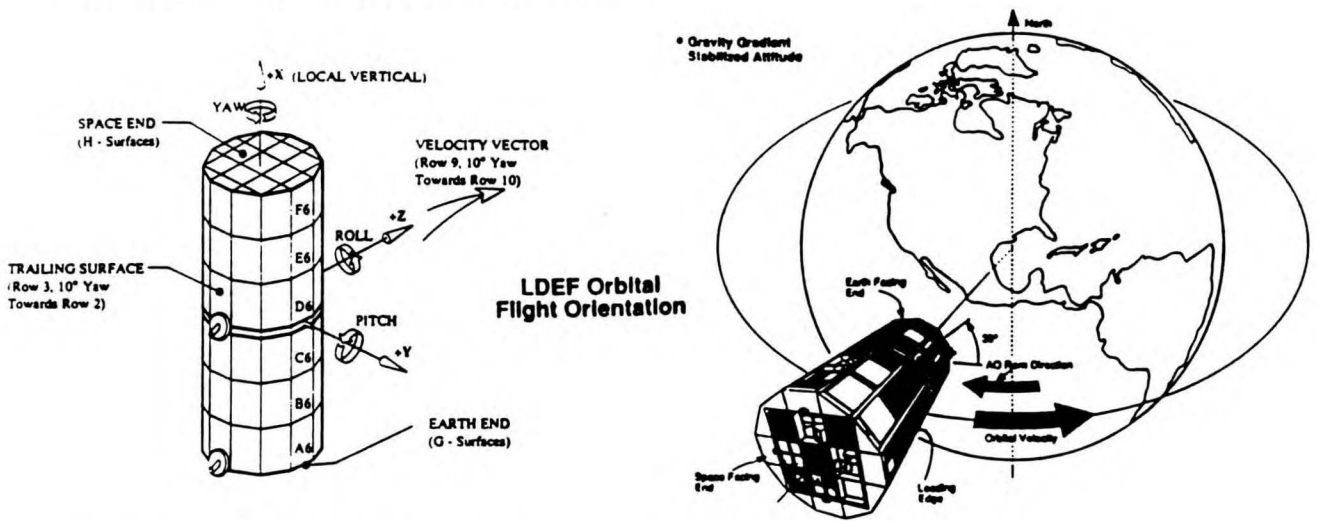


Fig-2 Long Duration Exposure Facility (LDEF)

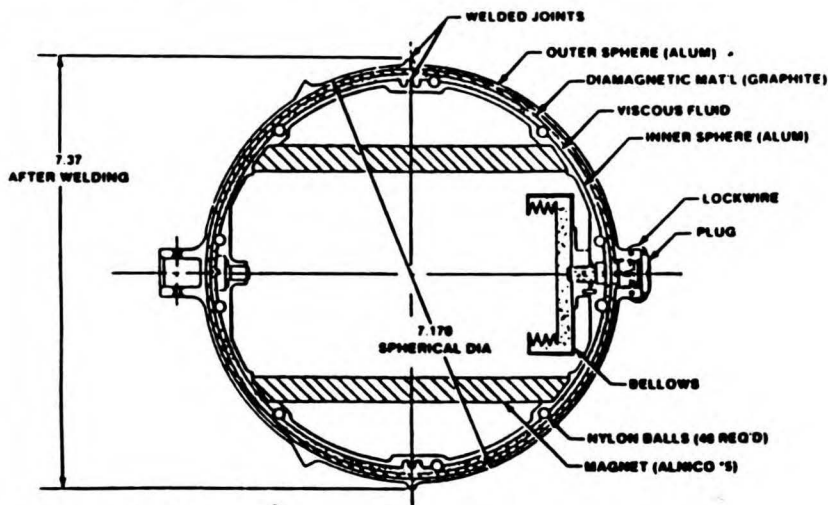


Fig-3 Passive Magnetic Damper

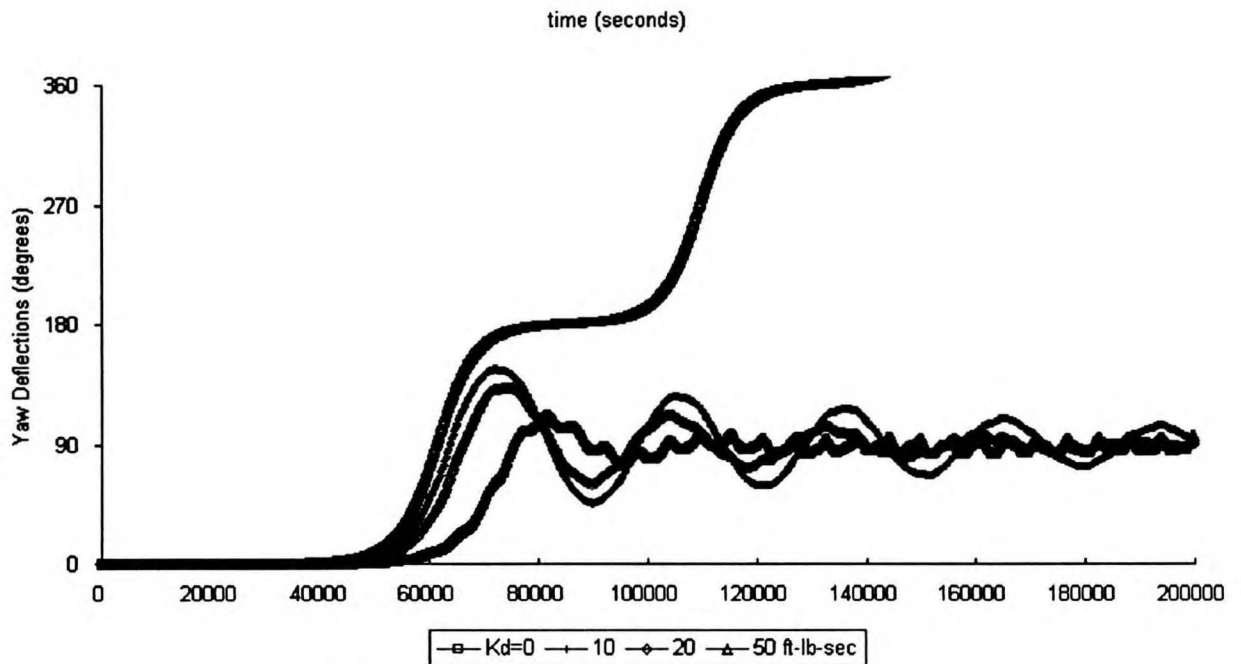


Fig.-4 Yaw Deflection Histories for Varied Damper Gains
 ET Simulated in Kepler Field, Principal Inertias Aligned to LVLH (X,Y,Z : R, N,T)
 Damper Gains $K_d = 0, 10, 20$ and 50 ft-lb-secs. Steady State for θ and ϕ ,
 ψ Wanders without Damper ($K_d=0$) or is aquired at Z alignment with N

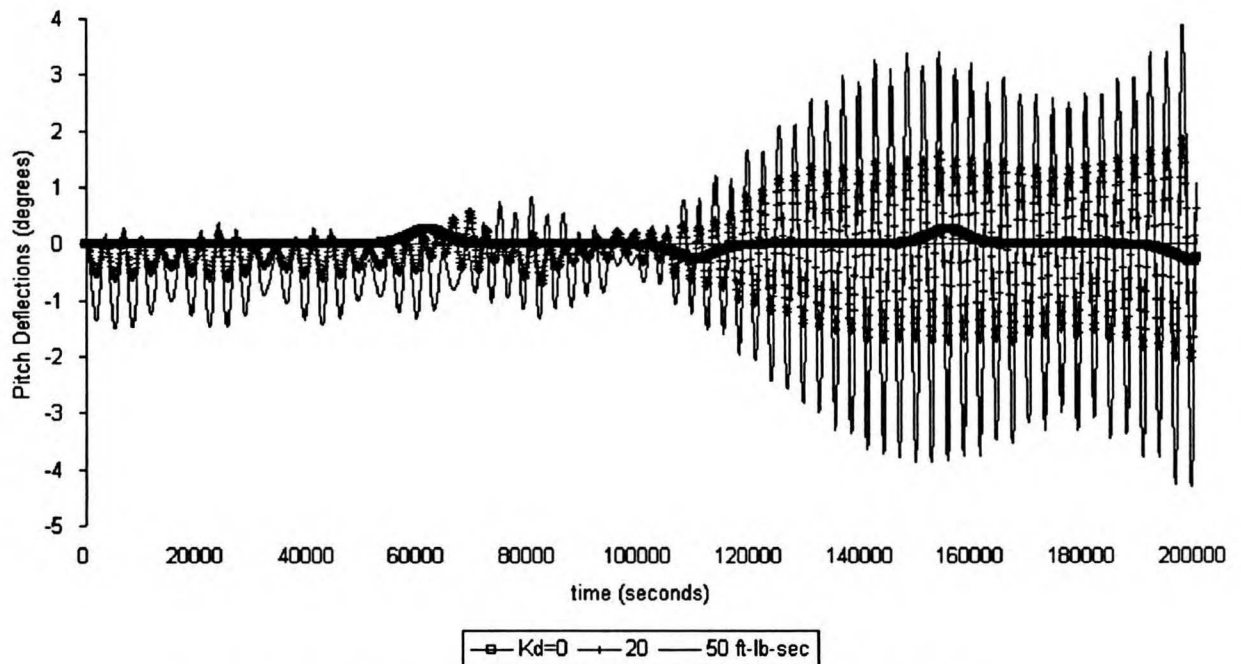


Fig.-5 Pitch Deflection Histories for Varied Damper Gains
 ET Simulated in Kepler Field, Principal Inertias Aligned to LVLH (X,Y,Z : R, N, T)
 Damper Gains $K_d = 0, 20$ and 50 ft-lb-secs. Steady State for θ and ϕ
 ψ Wanders without Damper ($K_d=0$) or is aquired at Z alignment with N

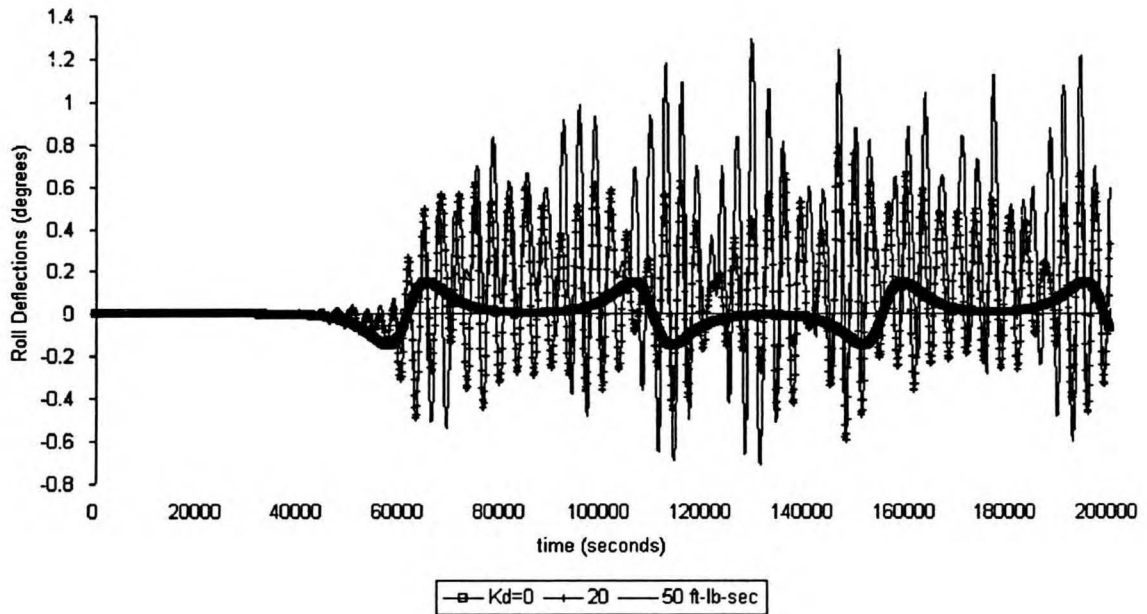


Fig.-6 Roll Deflection Histories for Varied Damper Gains
 ET Simulated in Kepler Field, Principal Inertias Aligned to LVLH (X,Y,Z : R, N, T)
 Damper Gains $K_d = 0, 20$ and 50 ft-lb-secs. Steady State for θ and ϕ
 ψ Wanders without Damper ($K_d=0$) or is aquired at Z alignment with N

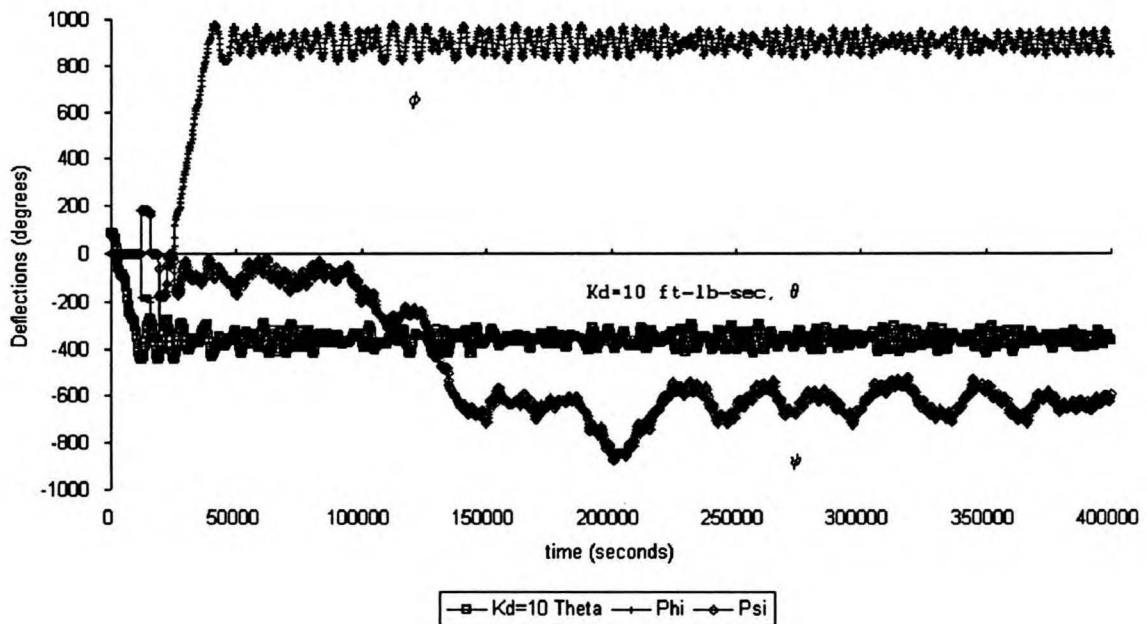


Fig.-7 Nominal ET-Separation with $K_d = 10$ ft-lb-sec
 ET Simulated in Kepler Field, Release dominated by $\sim 85^\circ$ Pitch Deflection

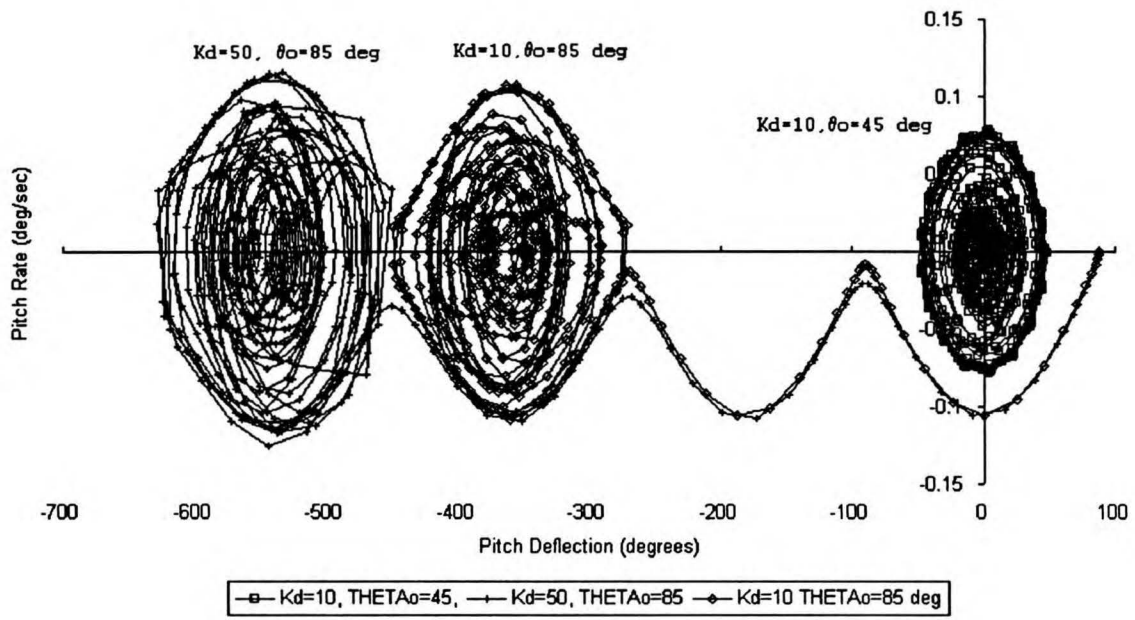


Fig.-8 Pitch Phase Plane, Varied K_d and Release Attitude
 ET Release with X axis and $\sim 85^\circ$ (Nominal) and 45° Deflection from R
 $K_d = 10$ and 50 ft-lb-sec, 144,000-sec Time Histories

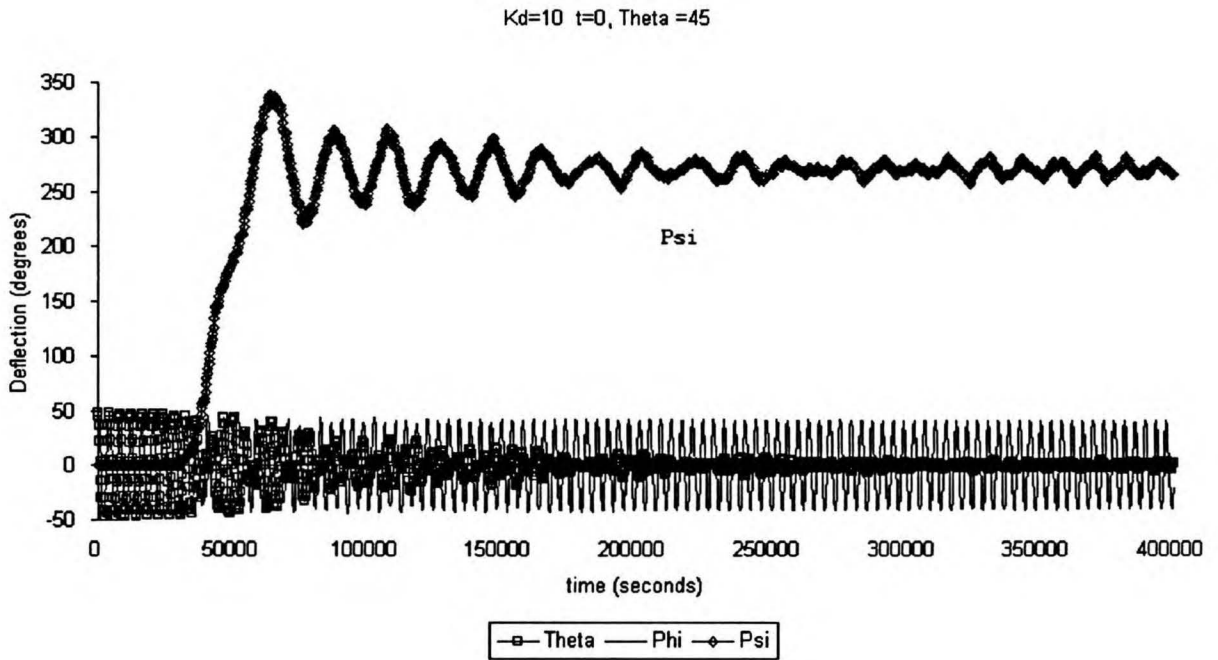


Fig.-9 ET-Separation with $K_d = 10$ ft-lb-sec, $\theta_0 = 45^\circ$
 ET Simulated in Kepler Field